

# A THERMAL RADIANCE MODEL FOR THE MOON AND MERCURY



Kay Wohlfarth, Christian Wöhler

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**Astronomy  
&  
Astrophysics**

# An advanced thermal roughness model for airless planetary bodies

## Implications for global variations of lunar hydration and mineralogical mapping of Mercury with the MERTIS spectrometer<sup>★</sup>

Kay Wohlfarth<sup>1</sup> , Christian Wöhler<sup>1</sup>, Harald Hiesinger<sup>2</sup> , and Jörn Helbert<sup>3</sup>

<sup>1</sup> Image Analysis Group, TU Dortmund University, Otto-Hahn-Str. 4, 44227 Dortmund, Germany  
e-mail: [kay.wohlfarth@tu-dortmund.de](mailto:kay.wohlfarth@tu-dortmund.de)

<sup>2</sup> Institute for Planetology, Wilhelm-Klemm-Str. 10, 48149 Münster, Germany

<sup>3</sup> Institute for Planetary Research, DLR, Rutherfordstr. 2, 12489 Berlin, Germany

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### ABSTRACT

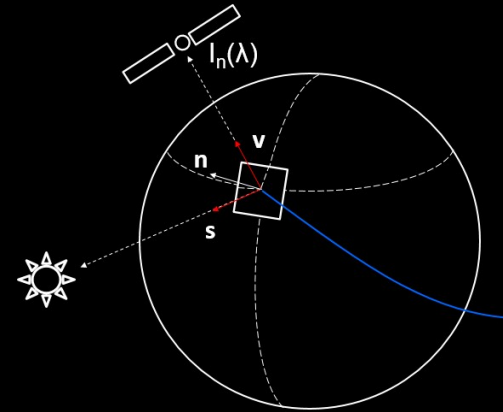
We present a combined reflectance and thermal radiance model for airless planetary bodies. The Hapke model provides the reflected component. The developed thermal model is the first to consistently use rough fractal surfaces, self-scattering, self-heating, and disk-resolved bolometric albedo for entire planets. We validated the model with disk-resolved lunar measurements acquired by the Chinese weather satellite Gaofen-4 at around 3.5–4.1  $\mu\text{m}$  and measurements of the Diviner lunar radiometer at 8.25  $\mu\text{m}$  and 25–41  $\mu\text{m}$ , finding nearly exact agreement. Further, we reprocessed the thermal correction of the global lunar reflectance maps obtained by the Moon Mineralogy Mapper M<sup>3</sup> and employed the new model to correct excess thermal radiance. The results confirm the diurnal, latitudinal, and compositional variations of lunar hydration reported in previous and recent studies with other instruments. Further, we compared the model to lunar measurements obtained by the Mercury Radiometer and Thermal Infrared Spectrometer (MERTIS) on board BepiColombo during a flyby maneuver on April 9, 2020: the measured and the modeled radiance variations across the disk match. Finally, we adapted the thermal model to Mercury for emissivity calibration of upcoming Mercury flyby measurements and in-orbit operation. Although a physical parameter must be invariant under various observation scenarios, the best lunar surface roughness fits vary between different datasets. We critically discuss possible reasons and conclude that anisotropic emissivity modeling has room for improvement and requires attention in future studies.

**Key words.** Moon – infrared: planetary systems – radiation mechanisms: thermal – methods: data analysis – methods: numerical – planets and satellites: surfaces

# Today

- Thermal model basics
- New: accuracy analysis
- New: comparison with more datasets
- Outlook

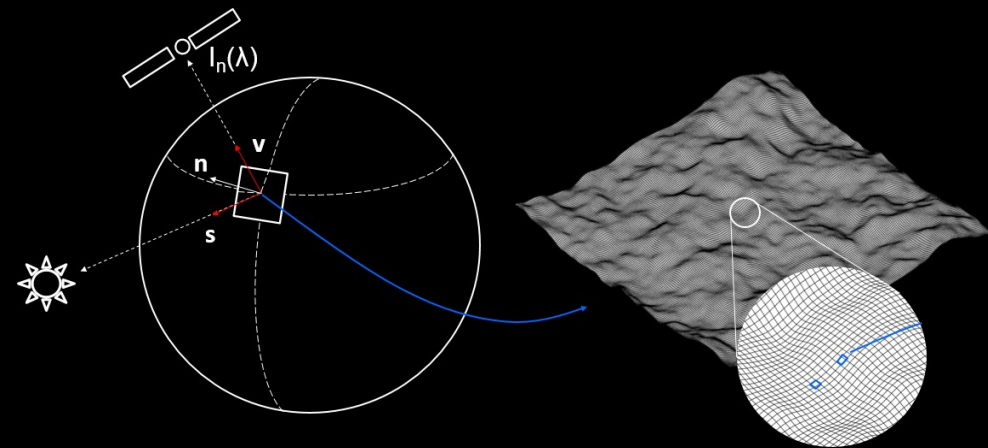
## Thermal Model 1/2



### Geometry

- Sub-solar point
- Sub-spacecraft point
- Solar distance
- Observer distance

## Thermal Model 1/2



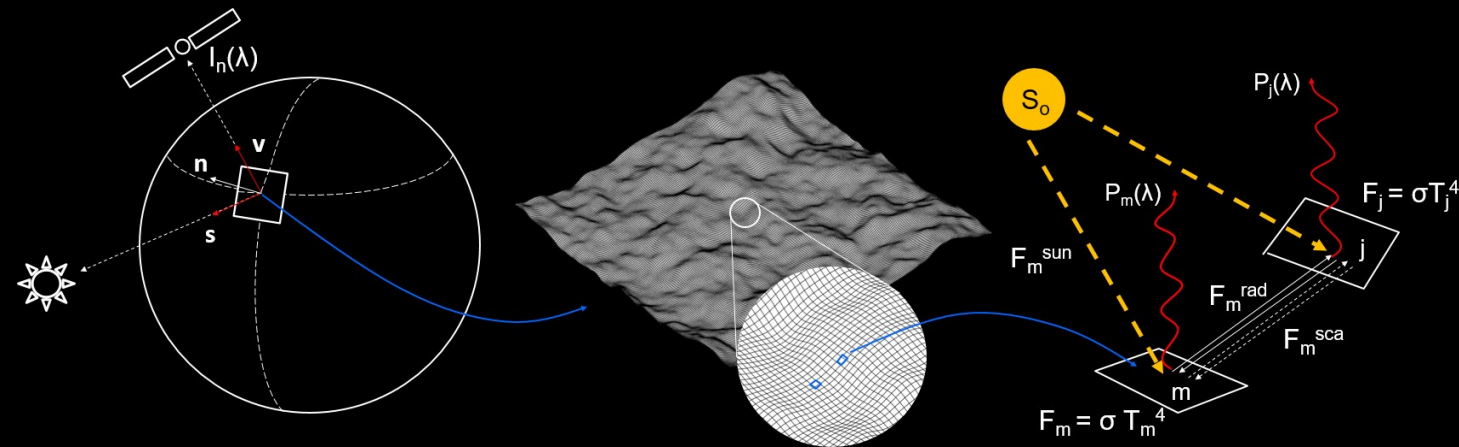
### Geometry

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### Surface

- Fractal  
Roughness  
 $\bar{\theta} = 30^\circ$
- Emissivity  
 $\varepsilon(\lambda, e)$

## Thermal Model 1/2



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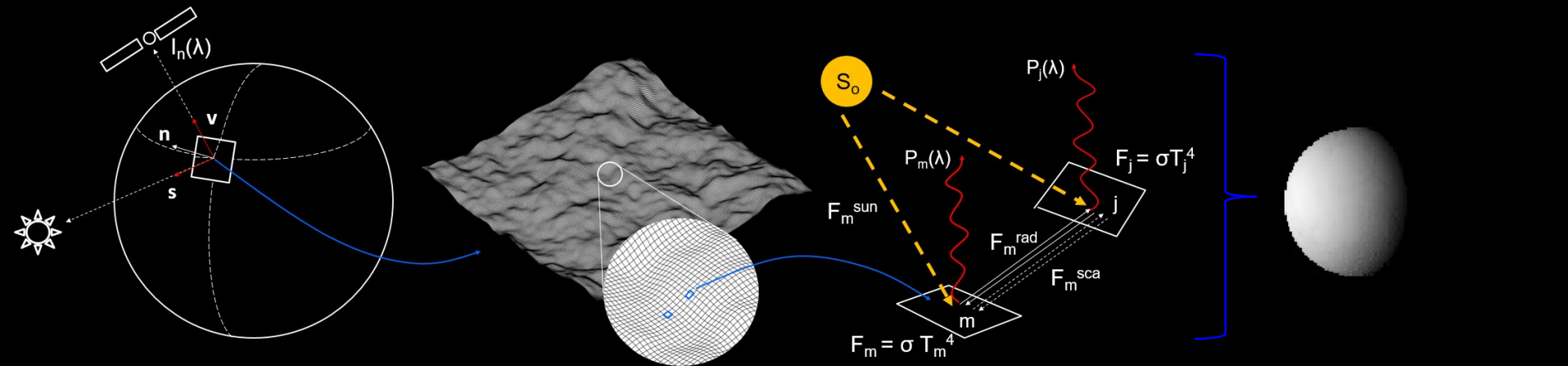
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### Model

- Self-scattering
- Self-heating
- Efficient linear algebra  $\rightarrow$  fast

# Thermal Model 1/2



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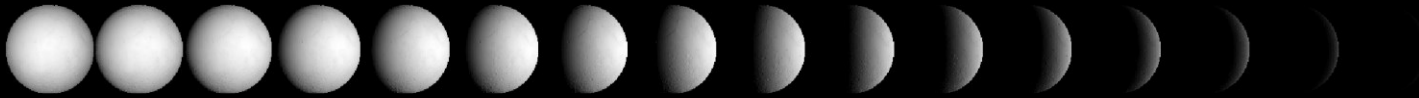
## Result

- Disk-resolved
- Projected
- Radiance  
[W/m<sup>2</sup>/μm/sr]

## Thermal model 2/2

$$\phi = 0^\circ$$

$$\phi = 180^\circ$$



- Disk-integrated simulations  
Consider the „usual suspects“
- Point/line spread function
  - Spectral response
  - Solid angle per pixel



## Datasets

- |                |                                     |                       |
|----------------|-------------------------------------|-----------------------|
| 1. Gaofen-4    | resolved, 4.8 $\mu$ m               | Wu et al. 2021        |
| 2. Diviner LRO | tracks, 8.25 $\mu$ m, 25-41 $\mu$ m | Bandfield et al. 2015 |

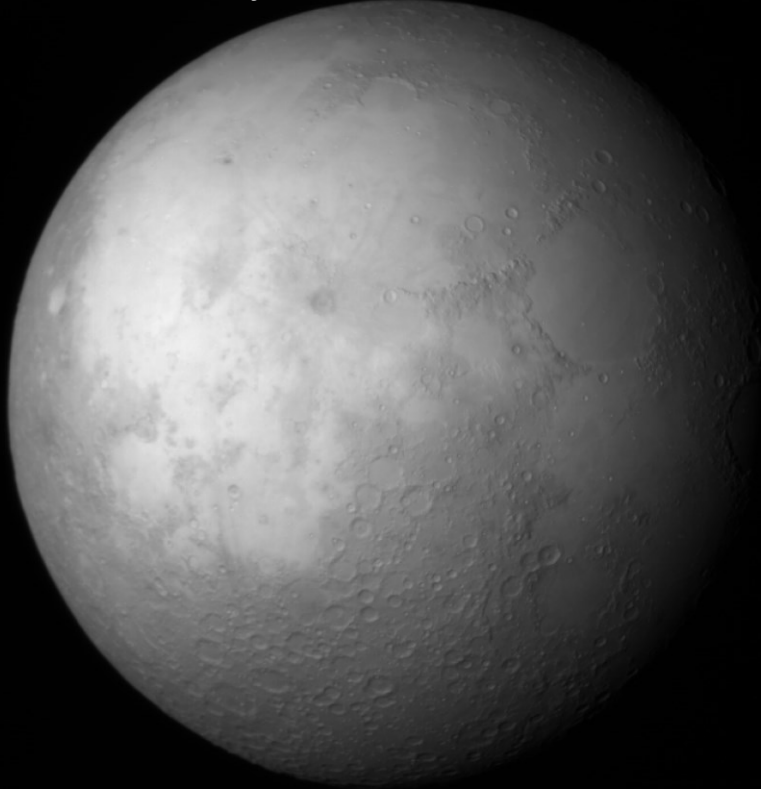
## Datasets

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| 3. HIRS-2/3/4 NOAA, MetOp | inegrated, 19 ch, 3-13 $\mu$ m      | Müller et al. 2021    |
| 4. FOREST-2               | resolved, 3.8; 8.8; 11.4 $\mu$ m    | Ororatech             |

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| 4. FOREST-2               | resolved, 3.8; 8.8; 11.4 $\mu$ m    | Ororatech             |
| 5. MODIS Aqua, Terra      | resolved, 6 ch, 3.6-12.3 $\mu$ m    |                       |
| 6. VIIRS J1, J2, NPP      | resolved, 5 ch, 3.6-12.5 $\mu$ m    |                       |
| 7. SLSTR Sentinel-3 A, B  | resolved                            |                       |

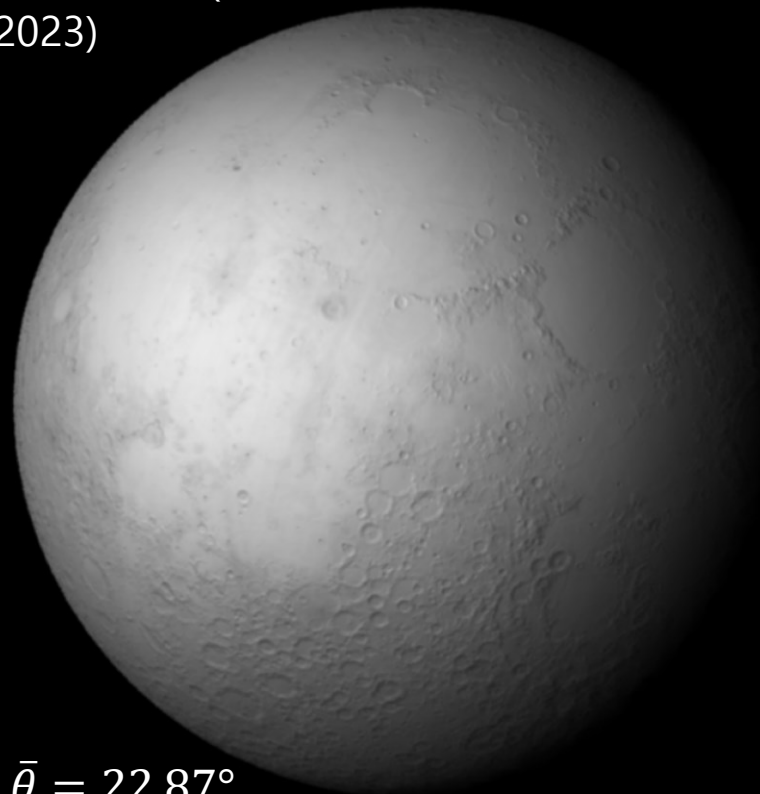
Measurement July 30, 2018 (Wu et al. 2018)



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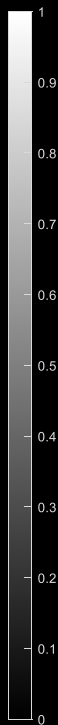


Our model (Wohlfarth et al.  
2023)



$$\bar{\theta} = 22.87^\circ$$

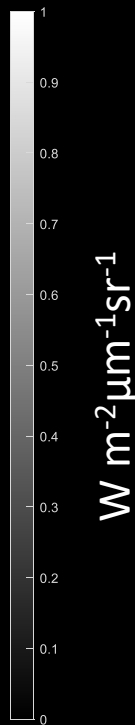
## RMSE between model and measurement for July 30, 2018



→ Avg. RMSE =  $0.2325 \text{ W m}^{-2} \mu\text{m}^{-1} \text{sr}^{-1}$

→ Avg. RMSE/max radiance = 2.91 %

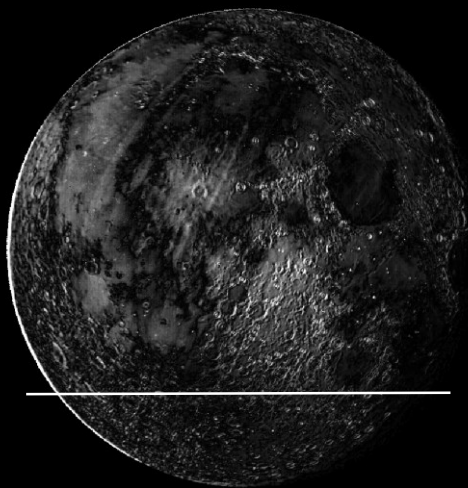
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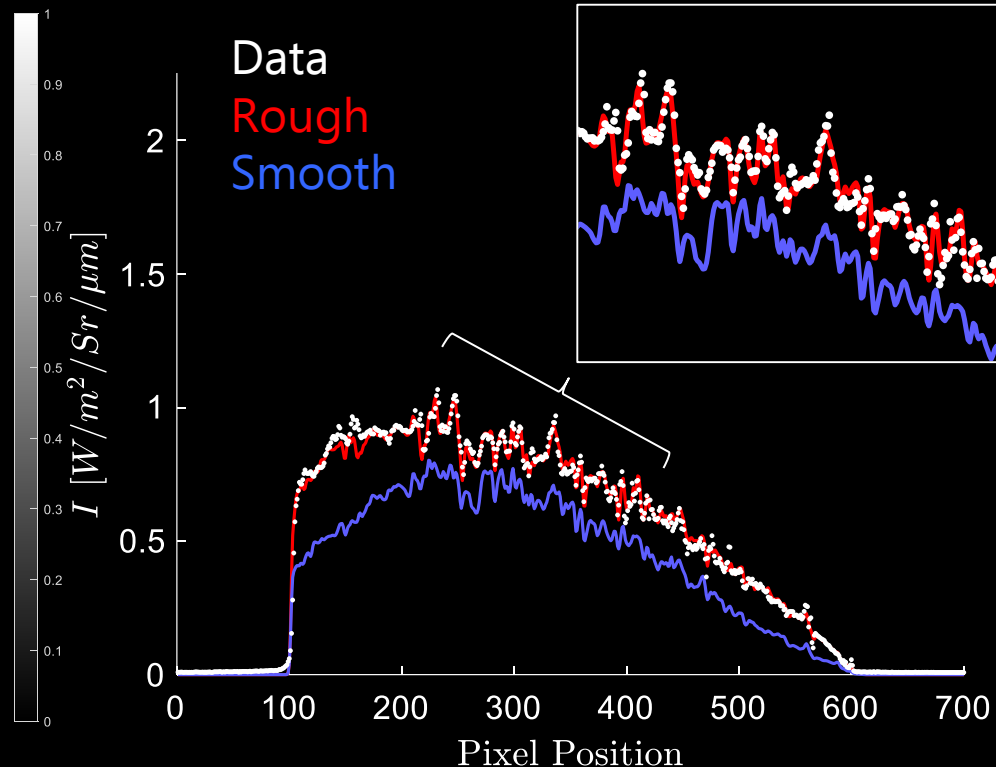
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RMSE between model and measurement  
for July 30, 2018



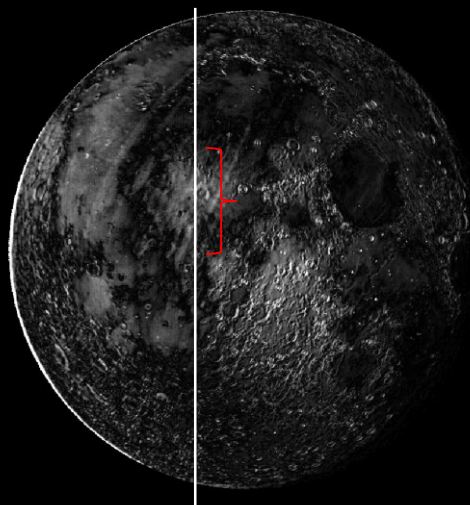
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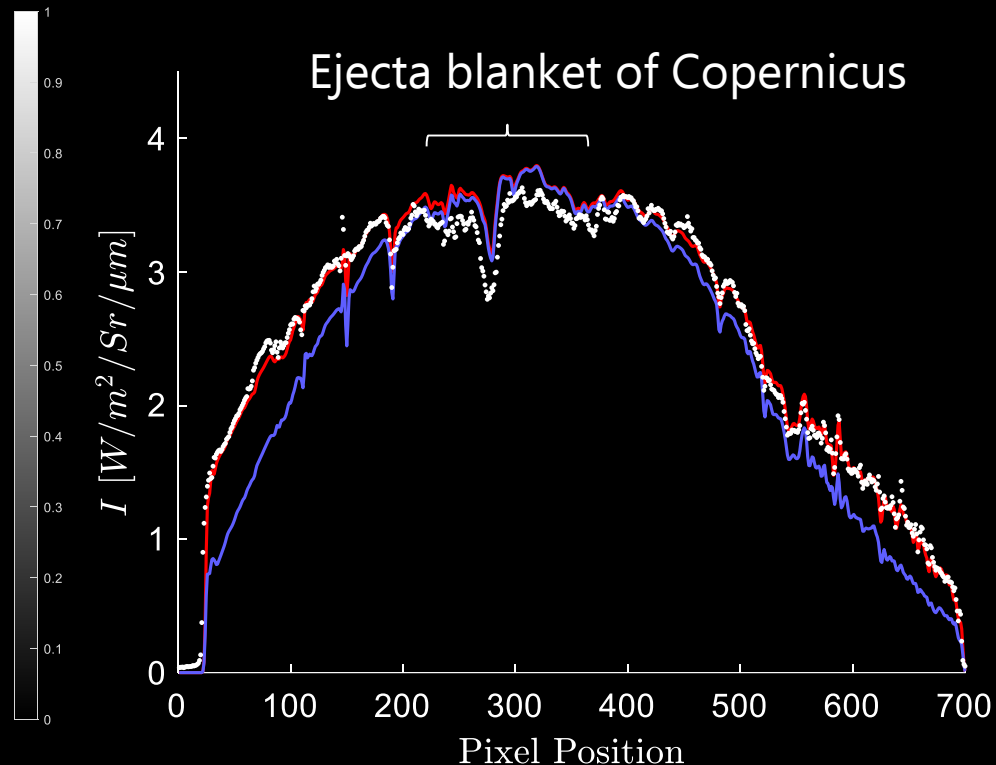


## RMSE between model and measurement for July 30, 2018

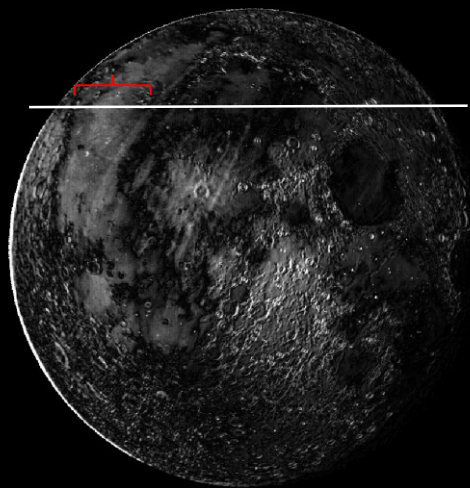


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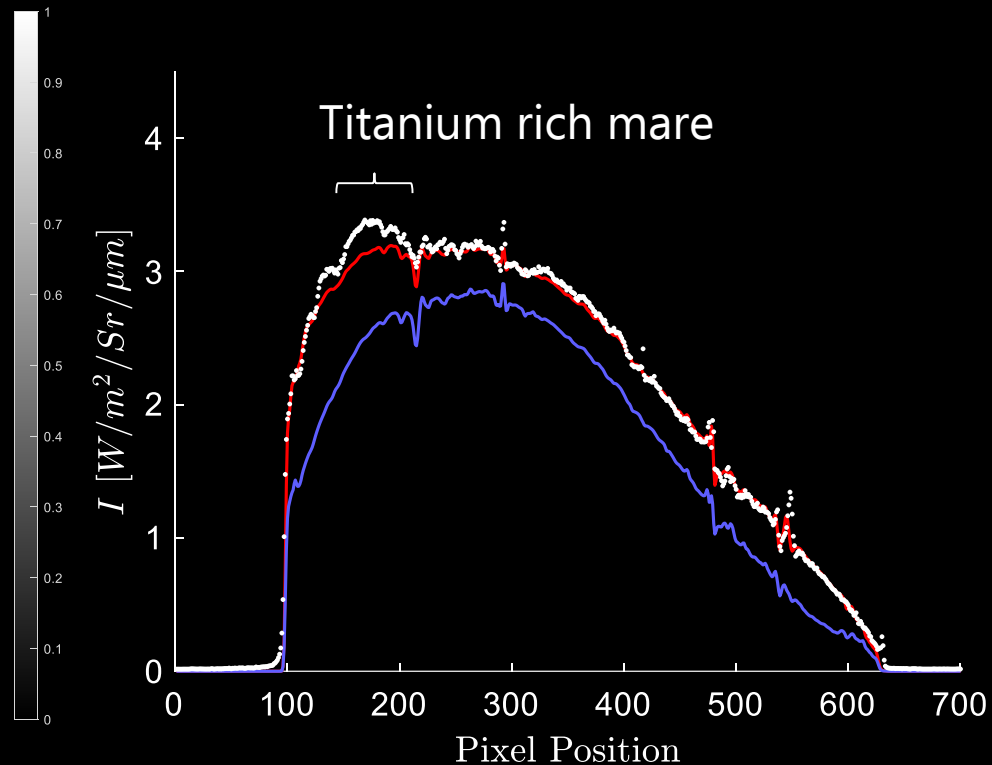


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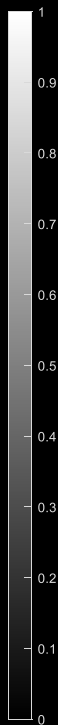


RMSE between model and measurement  
for July 30, 2018

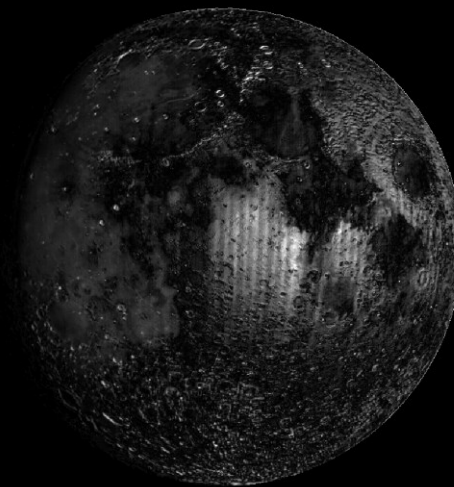


→ Avg. RMSE =  $0.2325 \text{ W m}^{-2} \mu\text{m}^{-1} \text{sr}^{-1}$   
→ Avg. RMSE/max radiance = 2.91 %

for July 25, 2018



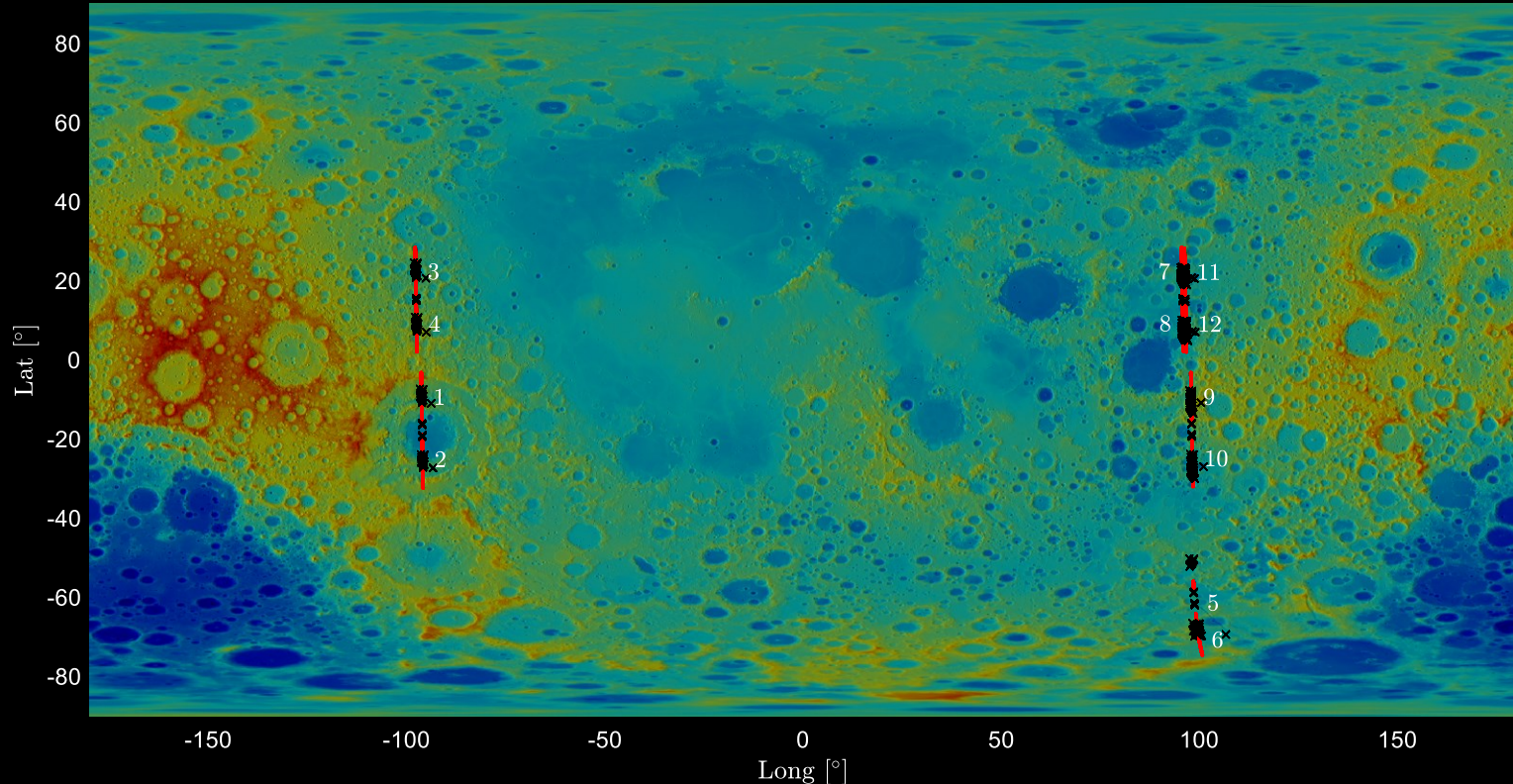
$\text{W m}^{-2} \mu\text{m}^{-1} \text{sr}^{-1}$

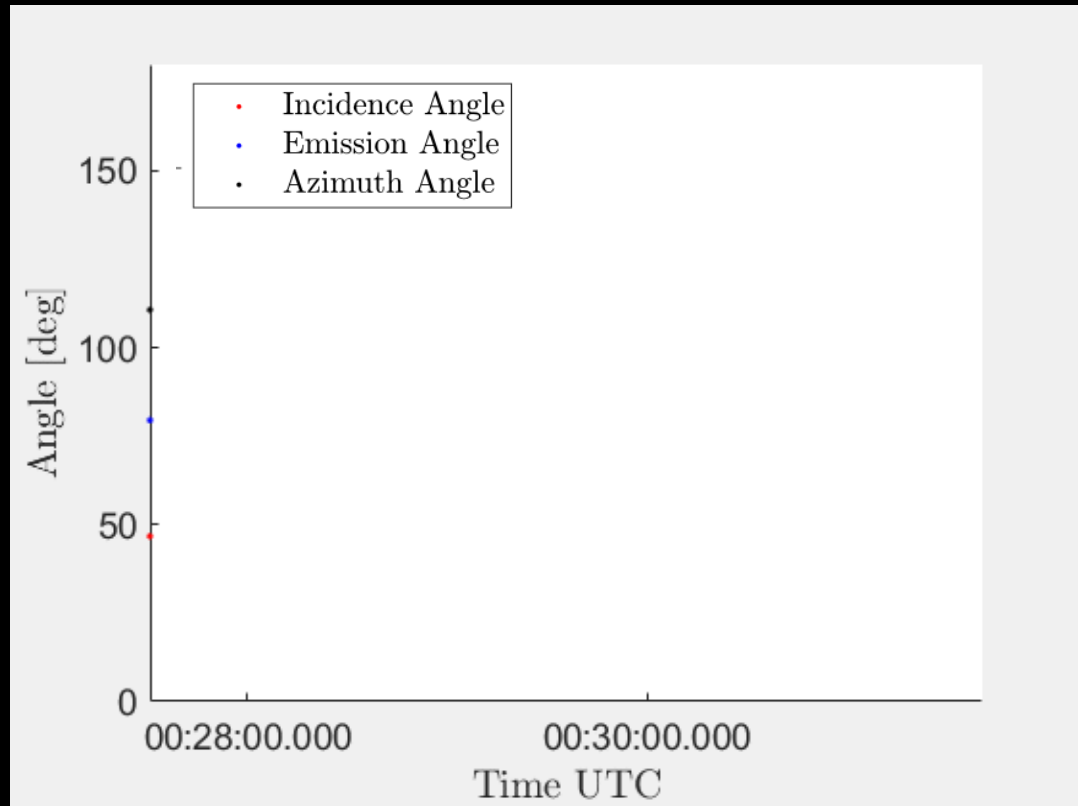
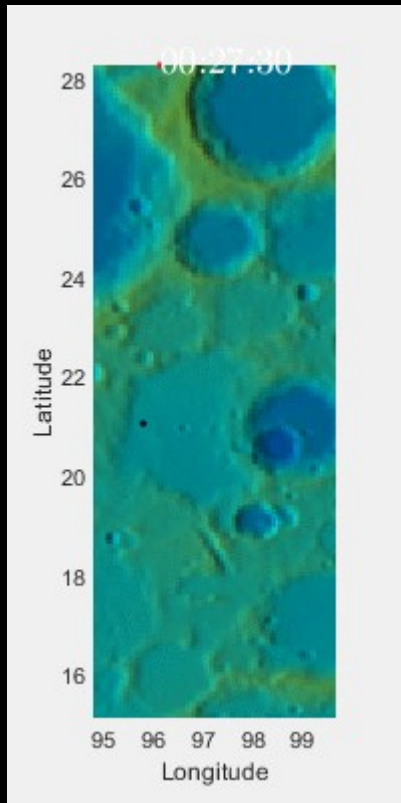


→ Avg. RMSE =  $0.1985 \text{ W m}^{-2} \mu\text{m}^{-1} \text{sr}^{-1}$   
→ Avg. RMSE/max radiance = 2.48 %

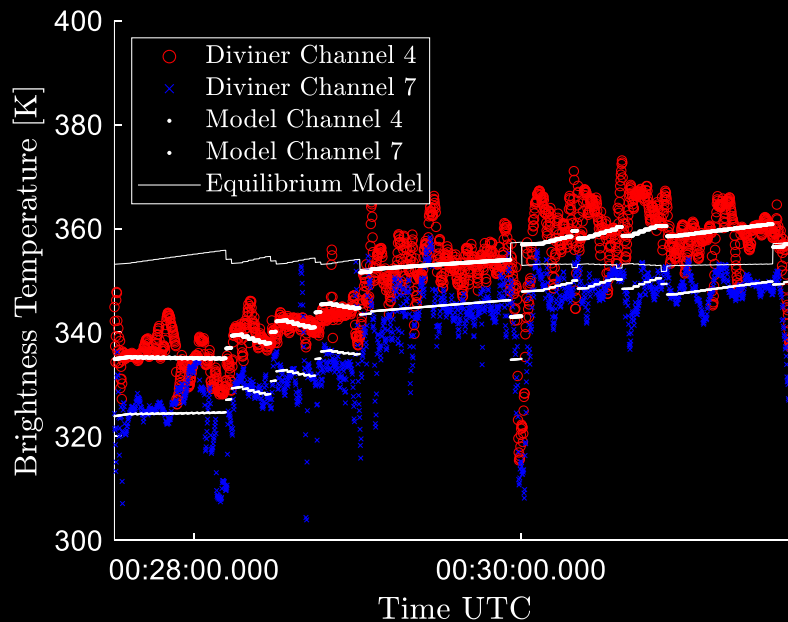
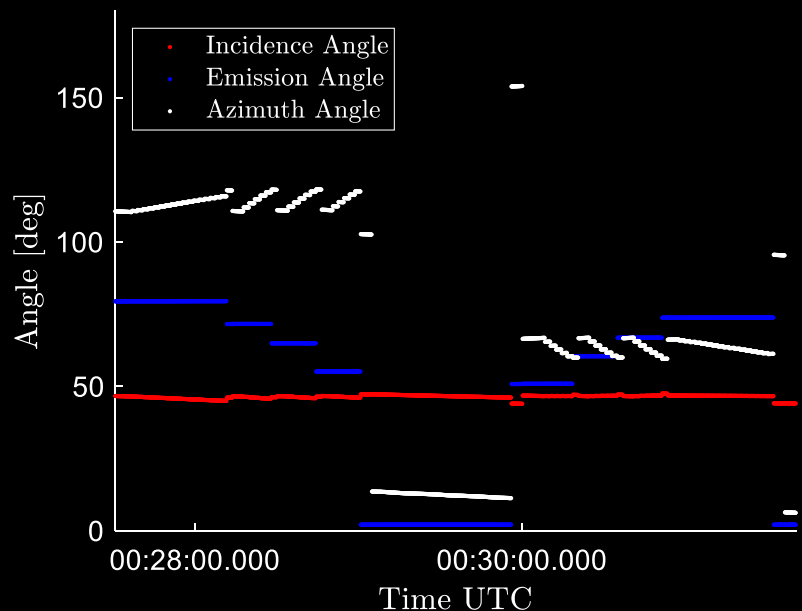
# Diviner EPF Measurements

Wohlfarth et al. 2023, EPF positions from  
Bandfield et al. 2015





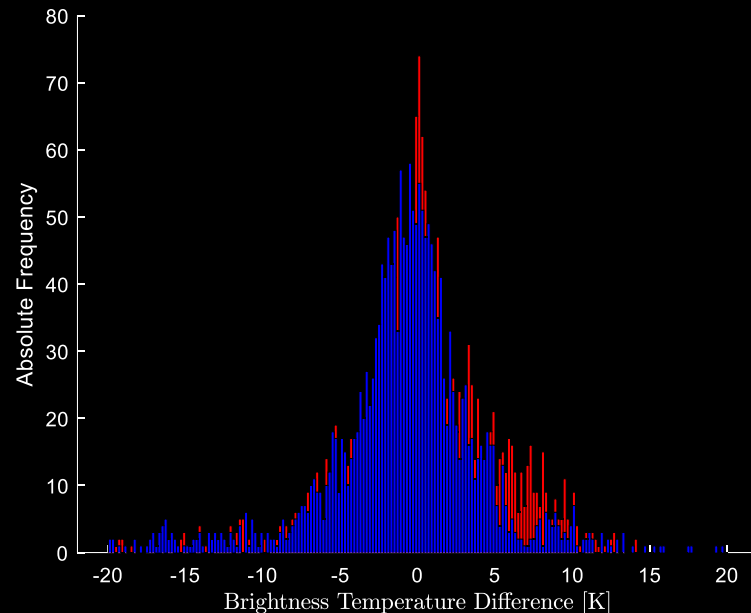
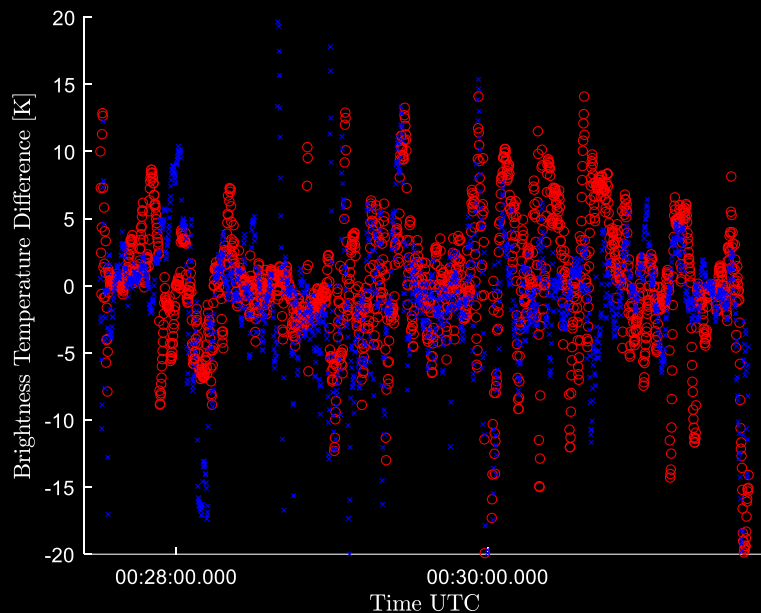
# Validation with Diviner: EPF



$$\bar{\theta} = 28^\circ$$



# Validation with Diviner: EPF

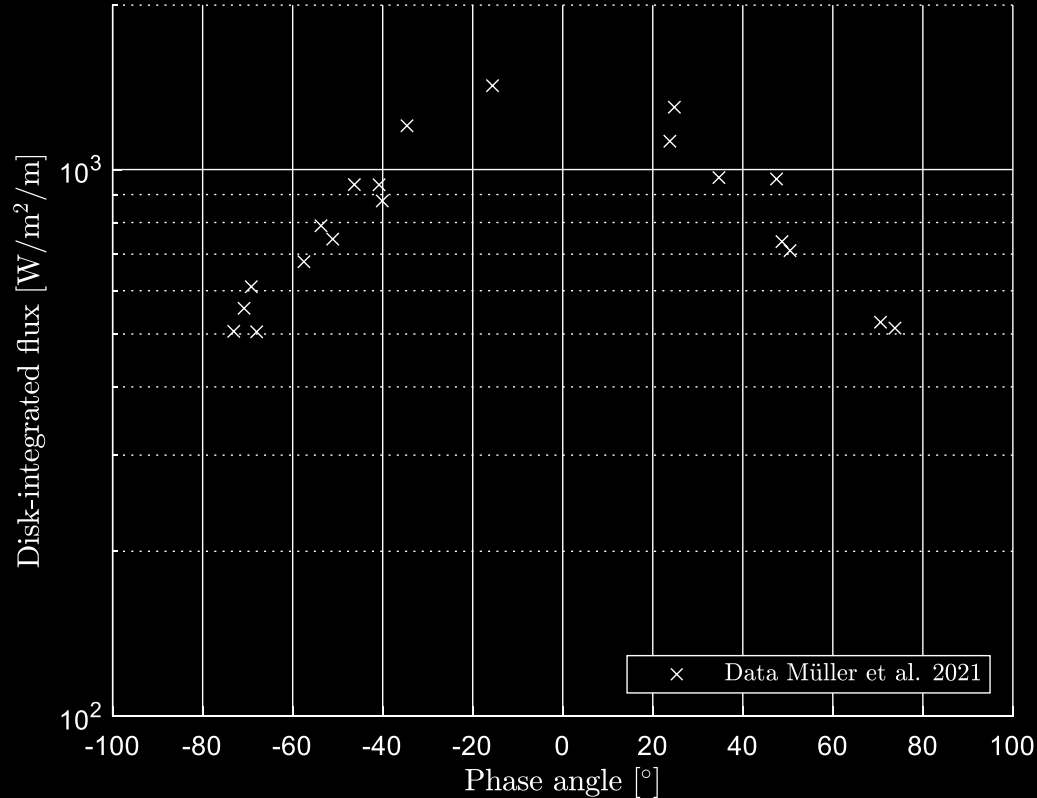


→ RMSE ch. 4 = 5.5982 K

→ RMSE ch. 7 = 6.1130 K

HIRS-2/3/4  
Channel 8  
11.1  $\mu\text{m}$

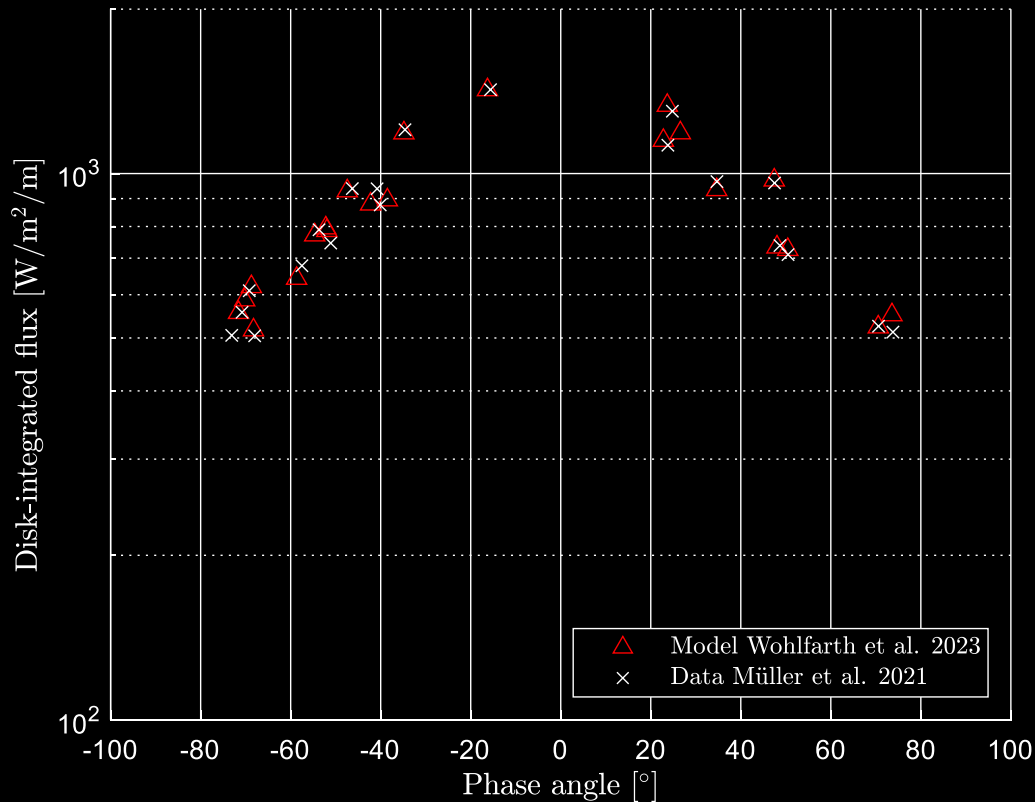
NOAA-11  
NOAA-14  
NOAA-15  
NOAA-17  
NOAA-18  
NOAA-19  
MetOp-A  
MetOp-B





HIRS-2/3/4  
Channel 8  
11.1  $\mu\text{m}$

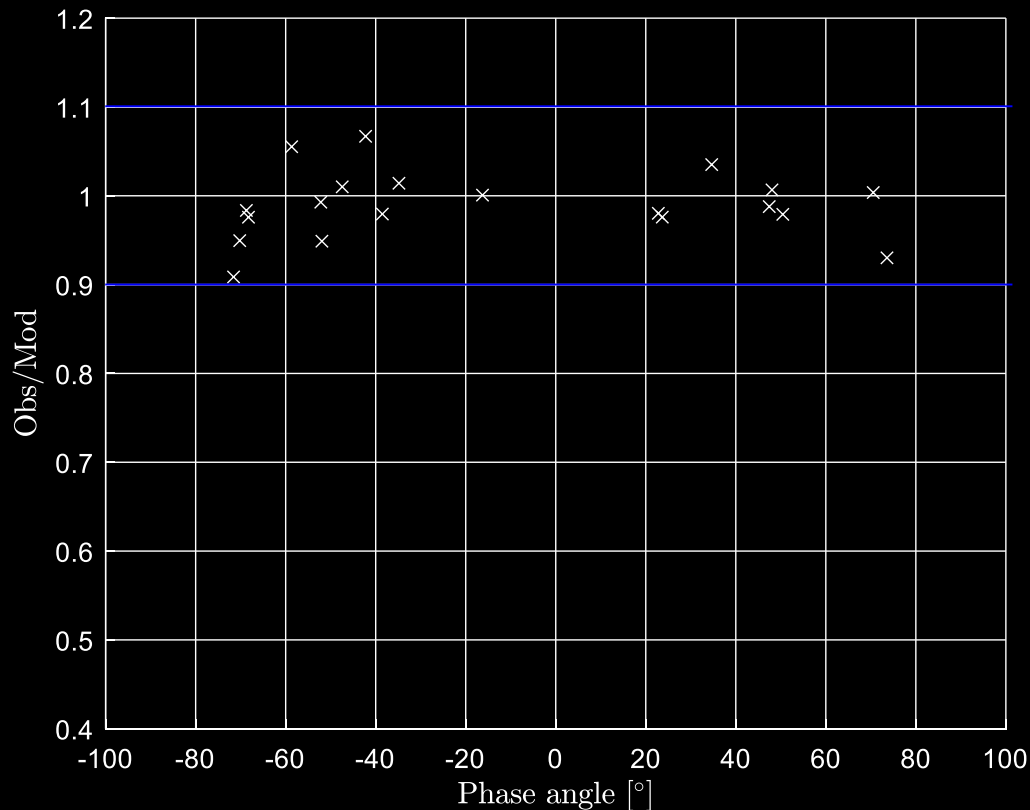
NOAA-11  
NOAA-14  
NOAA-15  
NOAA-17  
NOAA-18  
NOAA-19  
MetOp-A  
MetOp-B

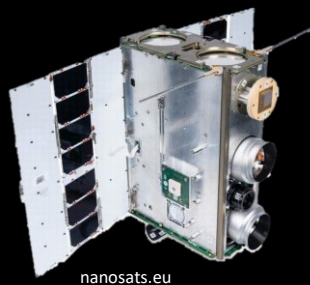


HIRS-2/3/4  
Channel 8  
11.1  $\mu\text{m}$

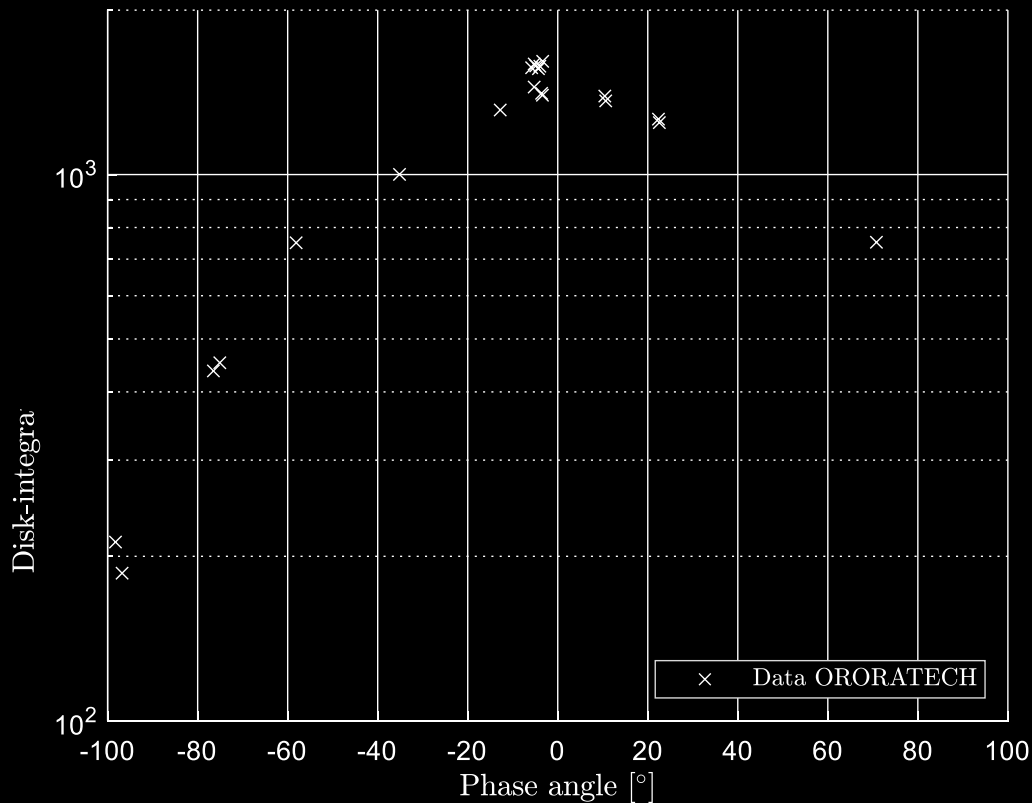
NOAA-11  
NOAA-14  
NOAA-15  
NOAA-17  
NOAA-18  
NOAA-19  
MetOp-A  
MetOp-B

Müller et al. 2021

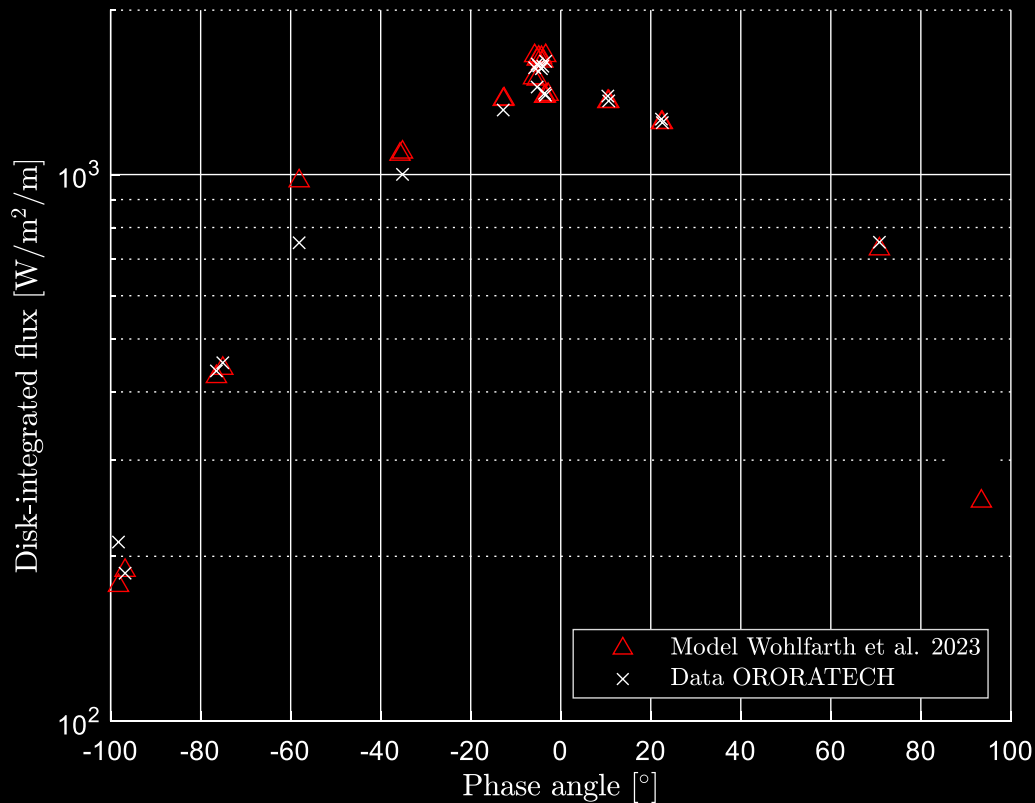




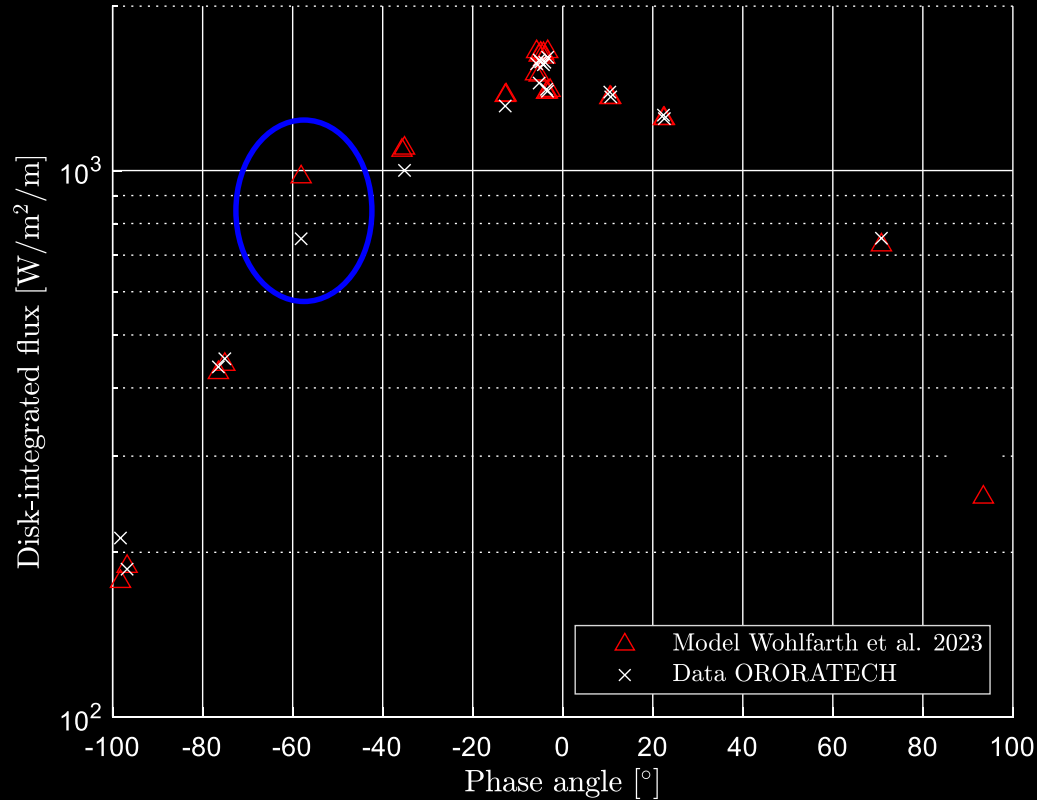
FOREST-2  
OroraTech  
LWIR band 2  
11.4  $\mu\text{m}$



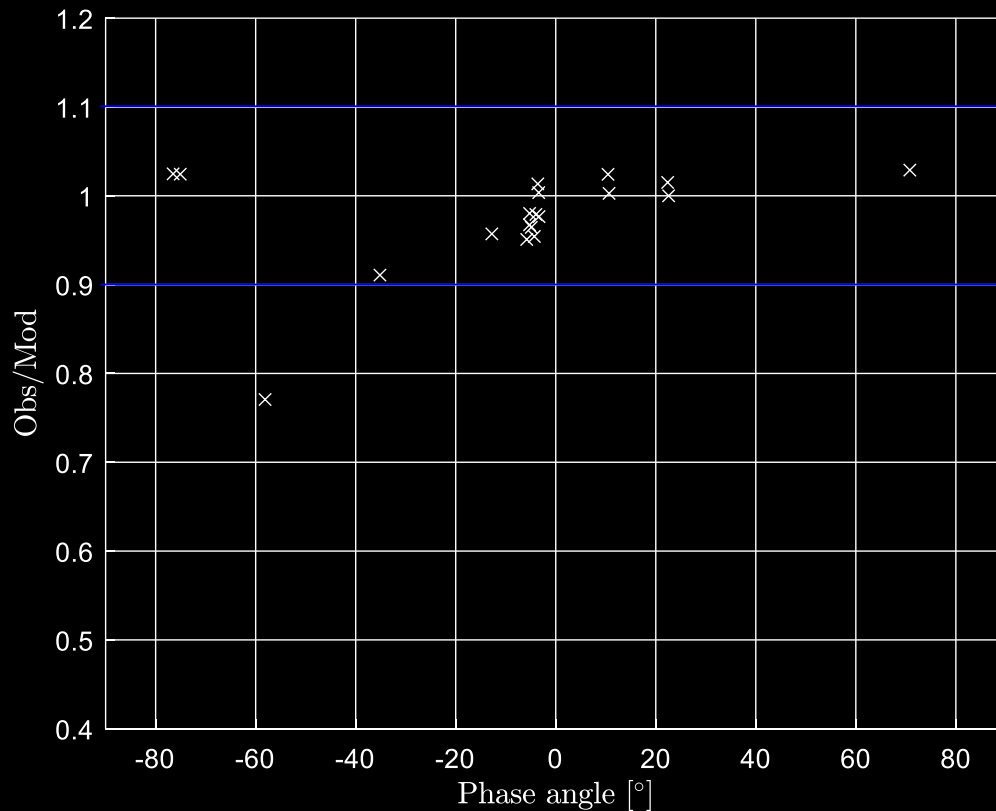
FOREST-2  
OroraTech  
LWIR band 2  
11.4  $\mu\text{m}$



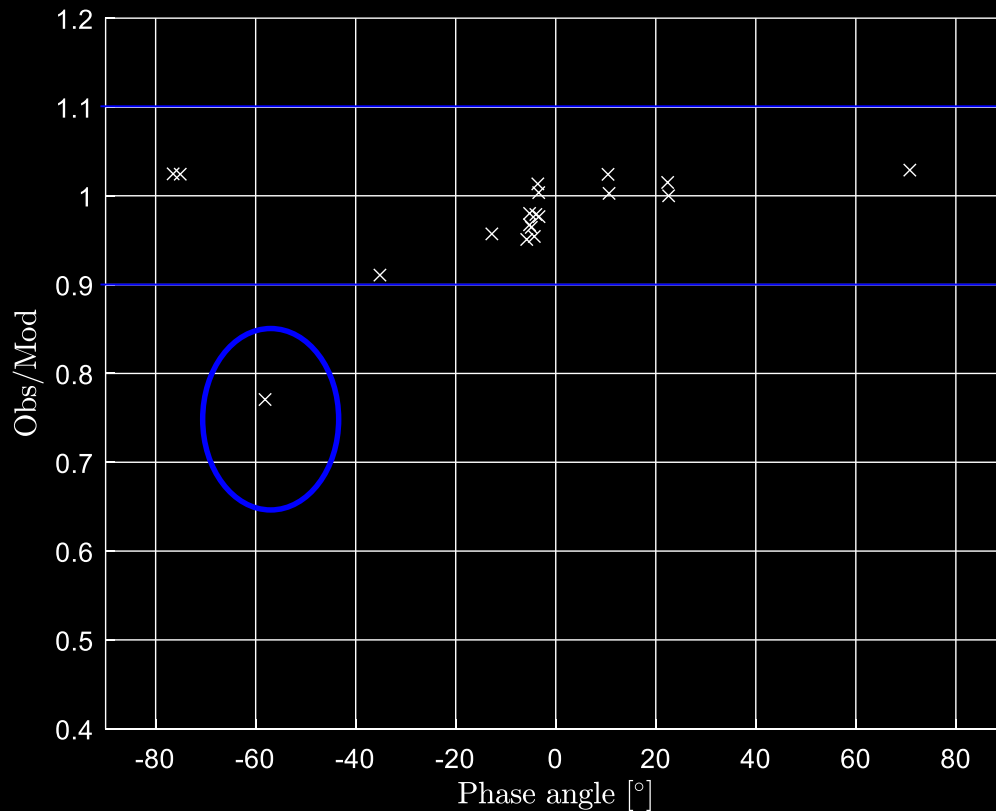
FOREST-2  
OroraTech  
LWIR band 2  
11.4  $\mu\text{m}$



FOREST-2  
OroraTech  
LWIR band 2  
11.4  $\mu\text{m}$



FOREST-2  
OroraTech  
LWIR band 2  
11.4  $\mu\text{m}$



## Conclusion

- Successful validation on the Moon (Gaofen-4 in MIR and Diviner in TIR)
- New comparison with HIRS-1/2/3 on NOAA and MetOp  
→ excellent agreement, also resembles Müller et al. 2021
- New comparison with ORORATECH Forest-2 L2 (11.4  $\mu\text{m}$ )  
→ Good agreement
- More datasets in the future!
- Get the interfacing right for professional use.